

Algebra II

11-3

Geometric Sequences

Geometric Sequence - terms vary by a common ratio (r)
(multiply or divide)

Example of an Geometric Sequence -

$$\begin{array}{ccccccccc} 5 & 10 & 20 & 40 & 80 & \dots & 1280 \\ a_1 & a_2 & a_3 & a_4 & a_5 & & a_n \end{array}$$

(Note: A blue bracket above the first two terms is labeled $r=2$)

Formula for finding the n^{th} term of an ~~Arithmetic~~ ^{Geometric} Sequence -

$$a_n = a_1 \cdot r^{n-1}$$

(Note: Red arrows point from labels to parts of the formula: "1st term" to a_1 , "ratio" to r , and "term number" to $n-1$)

Find a formula for the n^{th} term of each geometric sequence.

1) $2, 6, 18, 54, \dots$

$r=3$
 a_1

$$a_n = a_1 r^{n-1}$$

$$a_n = 2 \cdot 3^{n-1}$$

Find the specified term of each geometric sequence.

9) $320, 80, 20, 5, \dots; a_8$

$\sqrt{\div 4}$
 $r = \frac{1}{4}$

$$a_n = a_1 r^{n-1}$$

$$a_8 = 320 \left(\frac{1}{4}\right)^{8-1}$$

$$= 320 \left(\frac{1}{4}\right)^7$$

$$= 0.020 = \frac{5}{256}$$

Find the geometric mean of each pair of numbers.

19) $2, 8$

$\boxed{4}$

always positive

$r=2 \rightarrow 4 \rightarrow 8$

$2, 4, 8$
 $a_1, \quad a_3$

$$a_n = a_1 r^{n-1}$$

$$a_3 = 2r^{3-1}$$

$$8 = 2r^2$$

$$\sqrt{4} = \sqrt{r^2}$$

$$2 = |r|$$

Insert the given number of geometric means between each pair.

23) Three; $5, 80$

$5, 10, 20, 40, 80$
 $a_1, \quad a_5$

$$a_n = a_1 r^{n-1}$$

$$a_5 = 5r^{5-1}$$

$$80 = 5r^4$$

$$\sqrt[4]{16} = \sqrt[4]{r^4}$$

$$2 = |r|$$

Tell whether each sequence is arithmetic or geometric. Then find a formula for the n^{th} term.

29) $d = 8$ $+8$
 $25, 33, 41, 49, \dots, a_n$
 a_1

$$a_n = a_1 + d(n-1)$$

$$a_n = 25 + 8(n-1)$$

or

$$a_n = 25 + 8n - 8$$

$$a_n = 17 + 8n$$

either

Find a formula for the n^{th} term of each sequence. The sequences are neither arithmetic nor geometric.

37) $\frac{2}{1}, \frac{3}{4}, \frac{4}{9}, \frac{5}{16}, \dots, \frac{n+1}{n^2}$
 a_1, a_2, a_3, a_4, a_n

$$a_n = \frac{n+1}{n^2}$$

Assignment:

pg 513

2 - 38 even